

**Part 1: Introduction:** The sports boosters club is selling t-shirts and blankets at the football games to afford the charter busses that the team uses when traveling. T-shirts cost \$10 and blankets cost \$25. The booster club has set a goal of making \$2000 at each home game.

**How many T-shirts and blankets does the club need to sell in order to meet their goal?**

- a. Let  $x =$  # OF T-SHIRTS
- a. Write an expression for the amount of money raised from T-shirt sales:  $10x$

- b. Let  $y =$  # OF BLANKETS
- a. Write an expression for the amount of money raised from blanket sales:  $25y$

c. Write an equation that represents the sales goal:  $10x + 25y = 2000$

- d. Determine if the club will meet their goal if they sell 50 T-shirts and 50 blankets. Explain.
- Nope - \$250 short!
- $$50(10) + 50(25) = 500 + 1250 = 1750 \neq 2000$$

- e. Determine if the club will meet their goal if they sell 100 T-shirts and 40 blankets. Explain.
- Yes! It meets their goal exactly.
- $$10(100) + 25(40) = 1000 + 1000 = 2000 \checkmark (100, 40)$$

- f. Calculate two additional ordered pairs which would be solutions.
- g. Label the axes and graph the equation (use the ordered pairs or rewrite part c in function form).

T-SHIRT x	BLANKET y
100	40
200	0
0	80

$$10x + 25y = 2000$$

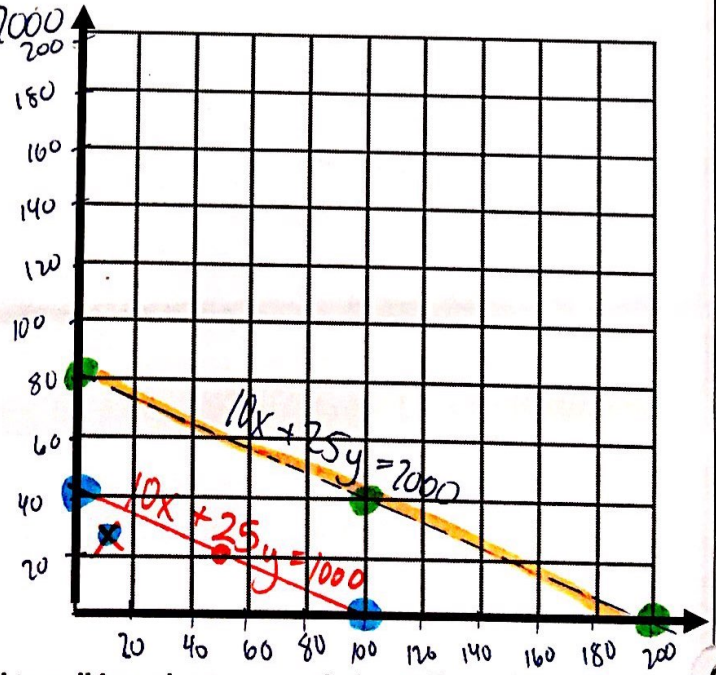
# BLANKETS

$$50(10) + 20(25) = 500 + 500 = 1000$$

$$10x + 25y = 1000$$

$$10(100) + 25(0) = 1000 \checkmark$$

x	y
100	0
50	25
0	40



So how many T-shirts and blankets does the club need to sell in order to meet their goal?

**MULTIPLE COMBINATIONS OF SHIRTS & BLANKETS.**



Part 2

a. At the away games, the club has a goal of earning \$1000. Create an equation that represents this goal.

$$10x + 25y = 1000$$

b. On the same coordinate plane as above in a different color, graph this equation.

c. Write each of the equations in function form:

Function 1:  $10x + 25y = 2000$   $\xrightarrow{-10x}$   $25y = -10x + 2000$   $\xrightarrow{\div 25}$   $y = -\frac{2}{5}x + 80$

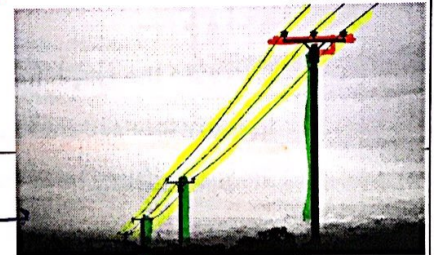
Function 2:  $10x + 25y = 1000$   $\xrightarrow{-10x}$   $25y = -10x + 1000$   $\xrightarrow{\div 25}$   $y = -\frac{2}{5}x + 40$

What do you notice about these equations?

Same Slope!

**Parallel Lines:** Two lines are parallel if

- They HAVE THE SAME SLOPE (different y-intercepts)
- They will NEVER (ever) INTERSECT



**Perpendicular Lines:** Two lines are perpendicular if they INTERSECT AT A 90° ANGLE.

\* SLOPES ARE OPPOSITE RECIPROCAL

Identify the kinds of lines you see in the image.

EX: if  $m_1 = \frac{7}{1}$ , so perpendicular line will have a slope of  $-\frac{1}{7} = m_2$

Example 1: Determine whether the graphs of each pair of equations are parallel, perpendicular, or neither. Explain your reasoning. Then, graph the equations to justify your response.

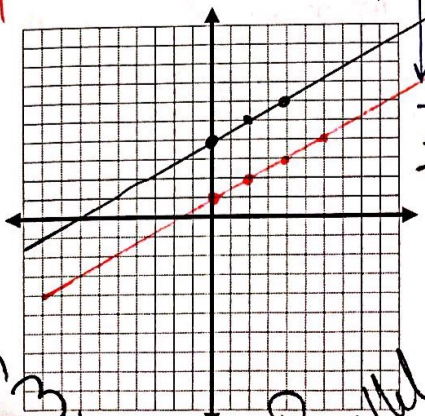
a. Get in function form

$$-2x + 4y = 4$$

to compare slopes

$$3x - 6y = -24$$

$$y = \frac{1}{2}x + 1$$



$$-3x - 6y = -24$$

$$-6y = -3x - 24$$

$$\frac{-6y}{-6} = \frac{-3x - 24}{-6}$$

$$y = \frac{1}{2}x + 4$$

Same Slope! → Parallel

b.

$$3x + 6y = 6$$

$$-2x + y = -3$$

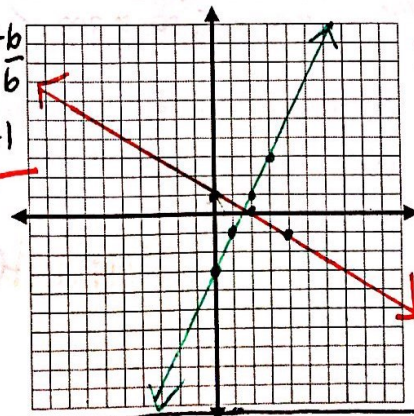
$$-3x - 6y = 6$$

$$+2x + 2x$$

$$\frac{6y}{6} = \frac{-3x + 6}{6}$$

$$y = -\frac{1}{2}x + 1$$

$$y = 2x - 3$$



SLOPES ARE OPPOSITE RECIPROCAL;  $m = -\frac{1}{2} \neq \frac{2}{1}$   
 ⊥ PERPENDICULAR LINES



Example 2: Find the slope of the line perpendicular to the equation of the line given; then, find the slope of a line that is parallel to the graph.

a.  $y = \frac{3}{2}x + 7$

Perpendicular:

$m = -\frac{2}{3}$

Parallel:

$m = \frac{3}{2}$

b.  $4x + y = 2$

$-4x$   $-4x$   
 $y = -4x + 2$

Perpendicular:

$m = +\frac{1}{4}$

Parallel:

$m = -4$

c.  $x - 3y - 8 = 0$   
 $-x + 8 -x + 8$

$-\frac{3y}{-3} = \frac{-x+8}{-3}$   $y = \frac{1}{3}x - \frac{8}{3}$

Perpendicular:

$m = -\frac{3}{1}$

Parallel:

$m = \frac{1}{3}$

d.  $y = -x$

$y = -1x$

Perpendicular:  $m = +$

Parallel:  $m = -1$

Part 3: The sports boosters club is selling t-shirts and blankets at the football games to afford the charter busses that the team uses when traveling. T-shirts cost \$10 and blankets cost \$25.

The booster club has set a goal of making at least \$2000 at each home game.

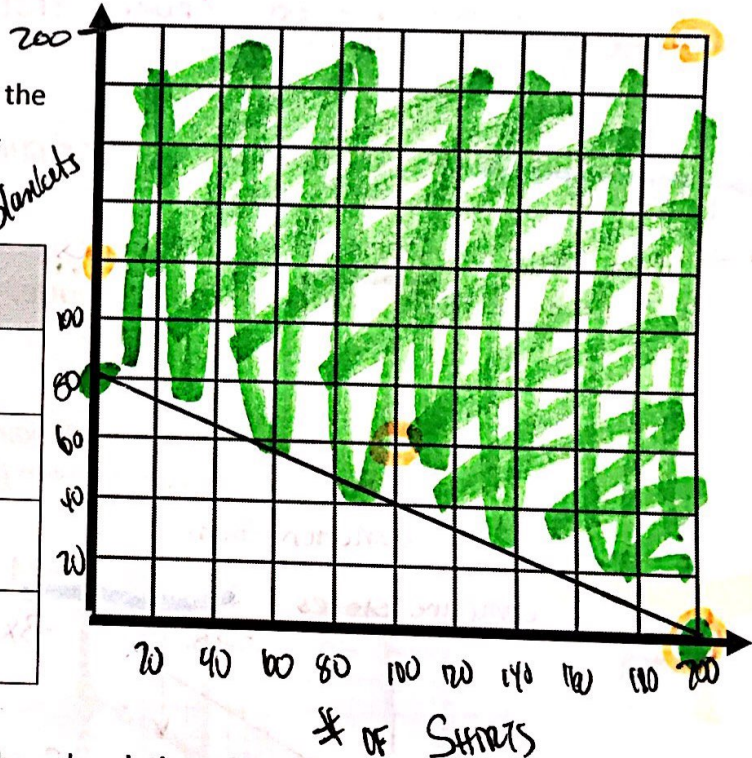
How many T-shirts and blankets does the club need to sell in order to meet their goal?

a. Compare the set up to part 1 to the set up of part 3.

$10x + 25y \geq 2000$

b. How would this be represented algebraically? Do so.

- c. Recreate the graph from the previous page.  
d. Identify four ordered pairs that are solutions to the inequality (they have to make a minimal sum of 2000).



x	y	Calculations that justify it's a solution.
0	120	$10(0) + 25(120) \geq 2000$ $3000 \geq 2000 \checkmark$
200	(0)	$10(200) + 25(0) \geq 2000$ $2000 \geq 2000 \checkmark$
100	60	$10(100) + 25(60)$ $1000 + 1500 \geq 2000 \checkmark$
200	200	$10(200) + 25(200)$ $2000 + 5000 \geq 2000 \checkmark$

e. Are the points that you identified on the graph the only solutions that make this inequality true? How many solutions are there?

Infinite!

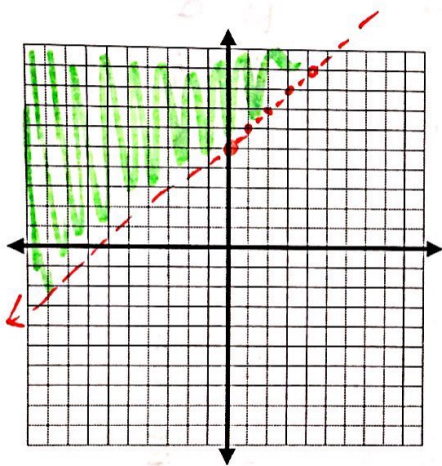


Graphing a two-variable linear inequality on a coordinate plane is similar to graphing a two-variable linear equation on a coordinate plane, except...

- Depending on the inequality symbol, the line could be...
  - $>$  or  $<$  → A DASHED LINE
  - $\geq$  or  $\leq$  → A SOLID LINE
- Depending on the inequality symbol, the region that represents the solutions....
  - $>$  or  $\geq$  ← GREATER THAN SHADE ABOVE
  - $<$  or  $\leq$  ← "LESS THAN" SHADE BELOW

How to graph a linear inequality in two variables:

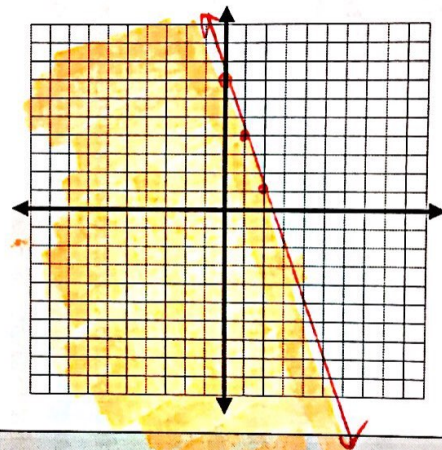
a.  $y > x + 5$   
 $\uparrow$   $\nwarrow$   
 $m=1$   $b=5$



1. If necessary, rewrite the inequality in FUNCTION FORM.  $y = \underline{\hspace{2cm}}$
2. Identify the SLOPE and y-INTERCEPT.
3. Plot the points for the boundary line.
4. According to the INEQ. sign, connect points with a DASHED or SOLID line.
5. Shade the SOLUTION region.  
 $>$  shade above  
 $<$  shade below

b.  $3x + y \leq 7$   
 $-3x$   $-3x$

$y \leq -3x + 7$

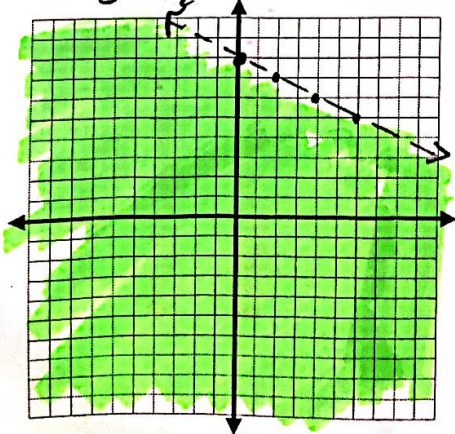


Examples: Graph the following inequalities.

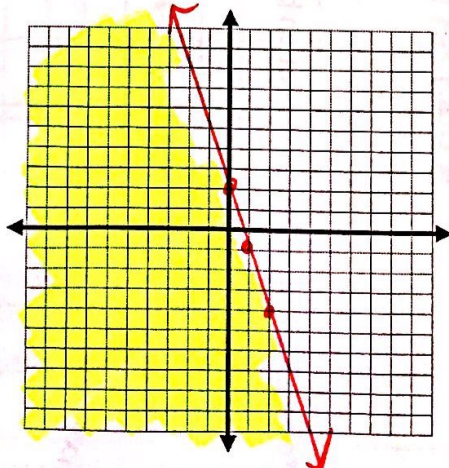
1.  $2x + 2y < 16$   
 $-2x$   $-2x$

$\frac{2y}{2} < \frac{-2x+16}{2}$

$y < -\frac{1}{2}x + 8$



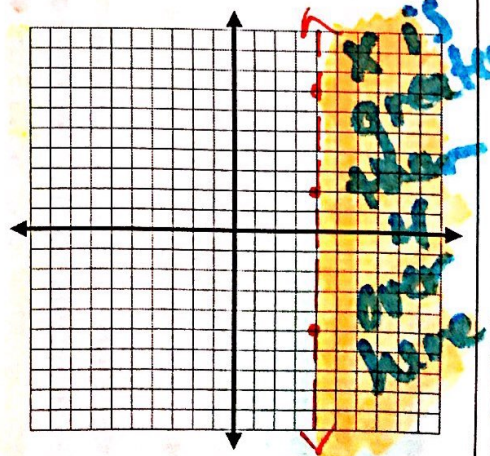
2.  $y \geq -3x + 2$



3.  $x > 4$

$x=4$

x	4	4	4
y	2	7	-5



Exit Ticket: Compare  $y > \frac{3}{2}x + 4$  and  $3y + 2x = 6$ .