

$$X = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

Algebra 1: Unit 4 Notes

Examples of applying the quadratic formula

1. $4x^2 + 3x - 5 = 0$
 $a = 4$
 $b = 3$
 $c = -5$

2. $2x^2 - 8x + 3 = 0$
 $a = 2$
 $b = -8$
 $c = 3$

$$x = \frac{-3 \pm \sqrt{3^2 - 4(4)(-5)}}{2(4)}$$

$$\sqrt{9 + 80}$$

$$x = \frac{-3 \pm \sqrt{89}}{8}$$

$$x = \frac{-3 \pm 9.4}{8}$$

Branch off \rightarrow
 $x = \frac{-3 + 9.4}{8} \rightarrow \frac{6.4}{8} = 0.8$

$$x = \frac{-3 - 9.4}{8}$$

$$x = \frac{-12.4}{8}$$

How to use the quadratic formula to solve a quadratic equation

1. Make equation = 0 using addition/subtraction.
2. Identify a, b, and c.
3. Substitute a, b, and c into quadratic formula.
4. Simplify expression under radical.
5. Simplify radical/evaluate radical.
6. Once numerator is simplified, solve for all solutions.

$$2x^2 - 8x + 3 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-8) \pm \sqrt{(-8)^2 - 4(2)(3)}}{2(2)}$$

$$\sqrt{64 - 24}$$

$$x = \frac{8 \pm \sqrt{40}}{4}$$

$$x = \frac{8 \pm 6.3}{4}$$

$$x = \frac{8 - 6.3}{4}$$

$$x = \frac{8 + 6.3}{4}$$

$$x \approx 0.4$$

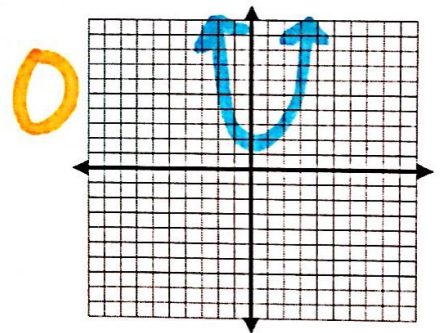
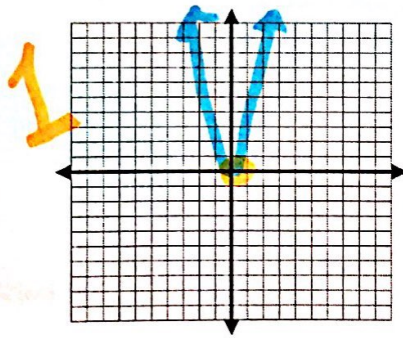
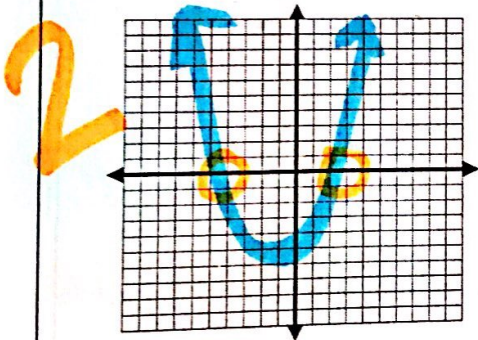
$$x \approx 3.5$$

Part 2:

What shape does a quadratic equation take when graphed?

parabola

If this graph was to slide around the coordinate plane, how many times could it possibly cross the x-axis?



What do you *have* to do when solving a quadratic equation (by factoring or by the formula)?

Keeping this in mind, where do you think the solutions are on a graph?

Solve = Roots =
 X-INTERCEPTS

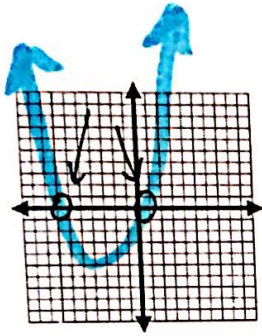
Discriminant, or $B^2 - 4AC$

is the part of the quadratic equation that leads to how many solutions the quadratic equation has.

If all you need to know is **how many** solutions a quadratic equation has, just use....

If $B^2 - 4AC = +$

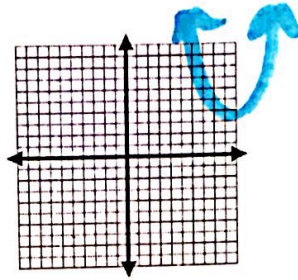
THERE ARE 2 REAL SOLUTIONS



$B^2 - 4AC$

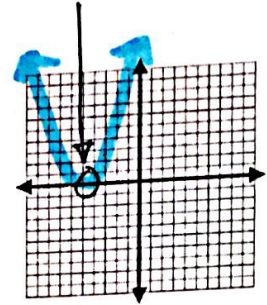
If $B^2 - 4AC = -$

THERE ARE NO REAL SOLUTIONS



If $B^2 - 4AC = 0$

THERE IS ONE REAL SOLUTION



How many real solutions does the equation have?

$4x^2 + 12x + 9 = 0$

$a = 4$

$b = 12$

$c = 9$

$B^2 - 4AC$

$12^2 - 4(4)(9)$

$144 - 144$

0

Since the discriminant = 0, there is one real solution

$5x = 2x^2 + 20$

$-5x \quad -5x$

$= 0!$

$a = 2$

$b = -5$

$c = 20$

$0 = 2x^2 - 5x + 20$

$B^2 - 4AC$

$(-5)^2 - 4(2)(20)$

$25 - 160$

Negative: no real solutions

$0 = 2x^2 + 15x - 28$

$a = 2$

$b = 15$

$c = -28$

$B^2 - 4AC$

$15^2 - 4(2)(-28)$

$225 + 224$

449

POSITIVE

2 REAL SOLUTIONS

Exit ticket: Imagine you were given a quadratic equation. List the order in which you would try to solve the equation.