

• infinite number of repetition

**Simulations**  
RECREATE A SCENARIO USING ONLY CHANCE BEHAVIOR TO CONTROL OUTCOMES

FINITE LIST

**Sample Space**  
• LIST OF ALL POSSIBLE OUTCOMES  
• TREE DIAGRAM

Law of Large Numbers: THE PROPORTION OF TIMES AN OUTCOME OCCURS IN MANY REPETITIONS WILL APPROACH A CERTAIN NUMBER

$P(x)$  event, value of desired event

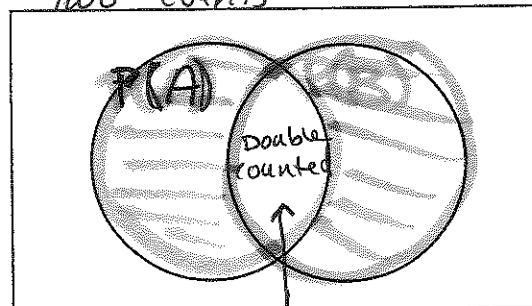
TWO + EVENTS

Some basic rules:  
 $0 \leq P(x) \leq 1$   
COMPLEMENT RULE  
 $P(A^c) = 1 - P(A)$   
"AT LEAST 1":  $1 - P(\text{none})$

**Probability**  
THE VALUE THAT IS APPROACHED VIA LAW OF LARGE #S

**Mutually Exclusive Events**  
• cannot occur simultaneously  
  
**Independent Events**  
• when knowing one outcome does not affect the chance of another

TWO events



General Addition Rule

Conditional Probability

$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$A \cup B$  "A or B"  
↑  
union of A and B  
• consists of all outcomes in A, in B, but not both  
  
 $A \cap B$   
↑  
intersection of A and B  
• "A and B"  
• Both A and B

PROBABILITY THAT AN EVENT HAPPENS, GIVEN ANOTHER HAS OCCURED.

$P(A|B) = \frac{P(A \cap B)}{P(B)}$   
↑  
given  
↓  
 $P(A \text{ and } B) = P(A|B) P(B)$

General Multiplication Rule

find probs that two events happen in sequence